

# Question Paper

Exam Date & Time: 05-May-2024 (02:30 PM - 05:30 PM)



## MANIPAL ACADEMY OF HIGHER EDUCATION

IV SEM B. Tech (BME) DEGREE END SEMESTER EXAMINATIONS, MAY-2024

SUBJECT: DIGITAL SIGNAL PROCESSING (BME 2225)  
(REVISED CREDIT SYSTEM)

May, 2024

**DIGITAL SIGNAL PROCESSING [BME 2225]**

**Marks: 50**

**Duration: 180 mins.**

### Descriptive

**Answer all the questions.**

Section Duration: 180 mins

Missing data if any can be assumed suitably.

Graphs have to be plotted on the sheets provided.

1A) Evaluate the 8-point DFT of the sequence  $x(n)=\{1,1,1,1,0,0,0,0\}$  using **Expansion method** (4)

1B) Compute the **circular convolution** for the given sequence  $x(n)$  and  $h(n)$  using **Stockham's method**. (4)

$$x(n) = \{1, 2, 2, 1\}$$

$$h(n) = \{2, 1, 2, 1\}$$

1C) Identify any two applications of DSP (2)

2A) Evaluate the 8-point DFT of the sequence. (4)

$x(n) = \{1, 2, -1, 2, 4, 2, -1, 2\}$  using the **radix-2 DIF-FFT algorithm**.

2B) A long sequence  $x(n)$  is filtered through a filter with impulse response  $h(n)$  to give an output response  $y(n)$ . (4)

If  $x(n)=\{1, 1, 1, 1, 1, 3, 1, 1, 4, 2, 1, 1, 3, 1\}$  and  $h(n)=\{1, -1\}$ . Evaluate  $y(n)$  using the **overlap-add method**. Use **only 5-point circular convolution** in your approach

2C) Compute the number of multiplications and additions needed for a **64-point sequence** in the calculation of DFT using the FFT algorithm and also find SIF (Speed Improvement Factor) (2)

3A) State and prove **circular time shifting** property of DFT (4)

3B) Realize the given system function  $H(z)$  in a **lattice ladder structure** (4)

$$H(z) = \frac{z^{-2} + 2z^{-1} + 1}{3z^{-2} + 3z^{-1} + 1}$$

3C) Realize the system function  $H(z)$  in **direct form structure for the given FIR filter** (2)

$$H(z) = 1 + \frac{1}{4}z^{-1} + \frac{1}{3}z^{-2} + \frac{1}{4}z^{-3} + \frac{1}{8}z^{-4} + \frac{1}{9}z^{-5} + \frac{1}{7}z^{-6}$$

- 4A) Design a **analog Butterworth low pass filter** with **-3dB** cut-off frequency at **500Hz** and attenuation of **(4) -15dB** at **750Hz**

(Refer to Table Q1 for the required data)

Q1) Data for Butterworth filter

<i>N</i>	<i>Normalised Denominator Polynomial</i>
1	$(1+s)$
2	$(1+1.414s+s^2)$
3	$(1+s)(1+s+s^2)$
4	$(1+0.765s+s^2)(1+1.848s+s^2)$
5	$(1+s)(1+0.618s+s^2)(1+1.618s+s^2)$

- 4B) A **digital low pass filter** is required to meet the following specifications. (4)

$$20\log|H(W)|_{W=0.2\pi} \geq -1.9328dB$$

$$20\log|H(W)|_{W=0.6\pi} \leq -13.9794dB$$

Design  $H(z)$  to meet the following specs using the **IIT (impulse invariant transform) method**.

(Refer to Table Q1 for the required data)

- 4C) If an input signal (2)

$$u(t) = 10 \cos(4\pi t) + \cos(40\pi t) + \sin(100\pi t) + 5 \sin(140\pi t)$$

$0 \leq t \leq 1$  is given to the ADC, **Compute** the Sampling frequency required to reproduce the signal, and also plot the rough FFT plot for the given signal

- 5A) Explain the **hamming window** used in the design of FIR filters. Draw the impulse response and magnitude response. (5)

- 5B) Realize the given digital filter equation using Direct Form 2 structure (3)

$$H(z) = \frac{(1 - \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2})}{(1 + \frac{1}{8}z^{-1} - \frac{1}{5}z^{-2} + \frac{1}{6}z^{-3})}$$

- 5C) Explain the **Design Procedure for BLT (Bilinear transformation) Method** with the help of a flowchart (2)

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